



Argument for Oort Cloud — in Modern Terms

- 1. Observations \implies We see ~ 1 'new' comet ($q < 5 \text{ AU}, H_{10} < 7$) discovered per year.
 - ▶ Semi-major axes $a > 2 \times 10^4$ AU: i.e. near parabolic limit; orbital
 - periods $P \simeq 3-30$ Myr short compared to age of solar system. These so-called 'new' comets strongly perturbed by Jupiter, so that
 - roughly half ejected, the remainder 'captured'. 'Captured' comets return, to be ejected or lost to short-period orbits
 - and eventual decay.
- 2. Conclude: All observed comets are ultimately lost; and the 'loss cone' affects all orbits with $q \lesssim 15$ AU. The loss timescale \ll age of solar system.
- 3. \implies comets are either a transient phenomenon, or there is a long-lived reservoir to replenish those that are lost.
- 4. Oort adopts primordial 'steady-state' hypothesis.

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View of Oort Cloud

- 1. Like a globular star cluster, such as M13..
 - Imagine Sun at centre
 - the stars become 'comets' the shape (like a flattened rugby
 - ball) is about right the strong concentration of comets towards the centre is
 - about right the overall dynamics is similar
- 2. Can calculate 'families' of Oort cloud models, in the same way as for star clusters and galaxies
- 3. External perturbations (e.g. stars) change cometary orbits

The 'loss cone' behaves just like the loss cone around a black hole in a galactic nucleus

Standard (1950) Model

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- 1. Assume: (1) spherical symmetry; outer radius $R_0 \simeq 200,000 \text{ AU}$; (2) random velocities, 'gardened' by stellar perturbations; (3) hydrostatic equilibrium (cloud neither expanding nor contracting); and (4) a simple energy distribution, e.g. a power-law distribution of orbital energies per unit mass $E = -GM_{\odot}/2a$
- 2. If $f(E) dE \propto |E|^{-\gamma} dE$, then the number density n(r) is roughly proportional to $r^{\gamma-4}$
- 3. Oort's (1950) model has $\gamma = 5/2$, corresponding to velocity space being uniformly filled at r up to a value V_{max} equal to the free-fill speed from R_0 to r. This implies $n(r) \otimes r^{-3/2}$, i.e. most of the mass near the outer edge.
- 4. Other models have smaller γ (e.g. $\gamma\sim$ 0), and much sharper inward density increases. The structure is much more like a dense star cluster, with a strong concentration of mass towards the centre, not a shell.
- 5. Leads to the concept of an inner Oort cloud, i.e. a Dense Inner Core: a region inaccessible to observation but possibly containing most of the cometary mass, and relatively safe from external perturbations.

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Further Details

- 1. 'New' comets are only lost if q lies within loss cone, i.e. $q \lesssim 15 \text{ AU}$; \Rightarrow Oort's reservoir must contain long-period comets of large q.
- $2. \ \mbox{For long-period orbits, planets change the orbital energy, i.e. change }$ 1/a, keeping q nearly constant; stars change the angular momentum, i.e. change q, keeping 1/a constant.
- 3. The change in q is about the size of the loss cone, provided the orbit is large enough.
 - Δq per revolution $\propto a^{7/2}$, i.e. depends sensitively on a.
 - > the reservoir must contain orbits of very long period
 - (a $> 2 \times 10^4\,{\rm AU},\,P > 5\,{\rm Myr})$ just like the observations Leads to Oort's idea of a nearly spherical cloud of comets with orbits extending up to halfway to nearest star.
- 4. The cloud is 'gardened' by various external perturbations.
 - including stellar, molecular cloud and large-scale systematic effects of Galactic tide.









Steps to Making Comets – I: Pre-Stellar Phase

- 1. Form dust grains in atmospheres of cool giant stars; eject to interstellar medium (ISM) via stellar winds.
- Cook in ISM for 10–1,000 Myr: complex cycling of grains through hot diffuse ISM, cool molecular clouds (MCs) and cold MC Cores.
 - In the clouds, grains accrete a frosting of interstellar volatiles; in the hot ISM, ice is sputtered and UV photo-processed; and grains are ground down by collisions and evaporation.
- Produce interstellar dust with a complex chemistry and broad size distribution; some grains have diameters up to microns or more.
- 4. Ices on <u>and within</u> the interstellar dust aggregates contain clues to the grains' previous history and to the processes that accompanied their 'final' pre-solar accumulation as part of the Sun's parent molecular cloud.
 - Cometary dust has a rich Cosmic Chemical Memory; cometary dust samples pre-solar history of solar-system material.

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Steps to Making Comets – IV: Growth Without Gas

- Dissipation of gas disc ⇒ further grain growth in absence of gas.
 Two main channels: (1) 'standard' planetesimal picture and variants therein (widely accepted); (2) local gravitational instability picture (much less widely accepted).
- 3. Consider (1) 'standard' planetesimal picture:
 - \blacktriangleright \implies continued collisions and growth of 'boulders'/'snowballs' to bodies up to several tens of km in protoplanetary zone.
 - Broduces up to several tension with in protopartically zone.
 Produces comets with collisionally evolved structure on scale of 'boulders' (i.e. ~10–100 m), and looser 'rubble-pile' structure on larger
 - (≳ km) scales; ⇒ comets collisionally evolved.
 Gravitational stirring by the largest bodies leads to continued growth, ultimately to make large planetesimals and planets.
- Problems: time-scale to produce Uranus and Neptunet.
 Problems: time-scale to produce Uranus and Neptunet.
 eads to need for migration models; Comets are planetary 'left-overs' formed in or close to outer planetary region, so total cometary mass should be not much greater than that of solids in the planets; role of planetary migration; roles of EKB and Oort cloud.
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Post-1990 Consensus

- 1. Comets are primordial solar-system bodies.
- 2. Formed by coagulation of originally interstellar dust grains during and after formation of protoplanetary disc.
- Coagulation proceeds rapidly in inner solar system, more slowly farther out (cf. Kant 1755); to produce the protoplanetary building blocks, namely: cometesimals and planetesimals.
- Late stages of planet formation involve (1) planetary and proto-planet collisions; (2) planetary migration (under mutual gravitational perturbations and evolution of protoplanetary disc); and (3) late-stage bombardment of planetary surfaces by comets and asteroids.
- Most work on origin of comets now focuses on (1) dynamical evolution of short-period comets; (2) simulations of origin and evolution of the Solar System and formation of Oort cloud; (3) origin of Centaurs, in the Jupiter-Neptune region and beyond; and (4) the structure and evolution of the trans-Neptunian region, i.e. the Edgeworth-Kuiper belt and beyond.
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- 1. Form the solar nebula from a rotating protosolar molecular cloud. It cools and collapses to produce a dense gas-and-dust disc.
- 2. Typical cloud parameters: Temperature $T \approx 10 \text{ K}$; Radius $R \approx 0.1 \text{ pc}$; Mass $M \approx 1-2 M_{\odot}$. Initial disc radius R_d small compared to R, but large compared to current planetary system. For reasonable parameters, $R_d \approx \text{few} \times 100 \text{ AU}$.
- Grains grow during nebular collapse and during disc evolution, acquiring a 'frosting' of ices from condensing volatiles in the MC core and protoplanetary disc.
- In the inner few AU of nebula, dust destroyed by collisions or by heating from the newly formed proto-Sun; dust farther out retains its Cosmic Chemical Memory.

By time Sun forms, expect grains with a complex 'hierarchical' structure, with evidence of both hot (pre-stellar) phases and cold (MC) phases of evolution.

Steps to Making Comets – III: Protoplanetary Disc Phase 1. Condensed ice composition: expect ices such as water, carbon monoxide, carbon dioxide, methanol, hydrogen cyanide, ammonia, methane etc.

- 2. Disc surface density Σ_d (solids) at 10 AU approximately 10 kg m⁻²; radial variation roughly a power law, i.e. $\Sigma_d \propto r^{-3/2}$. Gas-to-Dust ratio roughly 50 initially.
 - Surface density corresponds to a traditional 'minimum mass' protoplanetary disc within planetary region; total mass of solids within ~300 AU could range up to several 100 Earth masses.
- Initial grain growth proceeds rapidly in presence of gas through turbulence-driven coagulation. Large grains initially drift inwards due to gas drag and accrete smaller 'background' grains.
- 4. Grain radius versus time: $a(t) \approx 0.3 (100 \text{ AU}/r)^3 (t/1 \text{ Myr}) \text{ m}$. Thus, 'boulders', i.e. bodies with sizes up to $\approx 10-100 \text{ m}$, may form within 30 AU in a gas-clearance time-scale $\lesssim a$ few Myr, but probably much smaller objects — 'dirty snowballs' — farther out, i.e. sizes $\approx 1-10 \text{ m}$. Northumbria, NCL 2017 Sept 14 - #22

 The model predicts that comets are: (1) mostly made in outer solar system during evolution of subdiscs probably to produce multiple central objects;
 (2) the products of 'gentle' accumulation of 'boulders' or smaller 'snowball'-size components; and (3) therefore largely collisionally unevolved.

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Steps to Making Comets – V: Summary

- 1. Comets produced by hierarchical accretion in outer planetary system; final sizes range from a few km up to a few 100 km.
- 2. Cosmic Chemical Memory: interstellar and interplanetary dust aggregates contain ices that give clues to each of the distinct phases of grain growth in presence of gas, i.e. (1) interstellar gas and MC phases; (2) protostellar cloud and collapse phases; and (3) early disc evolution in presence of gas.
- 3. Evolution in absence of gas much more uncertain; but 'boulders' and/or 'snowballs' must somehow grow into kilometre-size (and larger) comet nuclei.
 - ► In planetesimal picture, comets collisionally evolved; mostly formed in protoplanetary region and may have rubble-pile structure with more compact elements on scale of 'boulders' (10-100 m).
 - In gravitational instability picture, comets collisionally unevolved and of low-strength; most formed beyond planetary region and may have substructure on scale of 'snowballs' ($\lesssim 10 \,\text{m}$ or less).

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New Discoveries: Pluto and Edgeworth-Kuiper Belt

- 1. Discovery of Pluto (1930 February 18), announced March 13.
- 2. Consistent with earlier speculations (e.g. Lowell) about a 'Planet X' beyond Neptune; or that small objects might exist in the region beyond Neptune (e.g. Campbell 1916, Aitken 1926, Leuschner 1927, Leonard 1930).
- 3. Stimulates work by Edgeworth (1938, 1943); and later by Kuiper (1951), Whipple (1964), Fernández (1980), Duncan et al. (1988), Quinn et al. (1990) and others, focusing on <u>JF</u> short-period comets.
- 4. Searches by Kowal (1976–1985), Luu & Jewitt (1988), Levison & Duncan (1989), Tyson et al. (1992), eventually successful. Discovery of 'QB1', i.e. minor planet (15760) 1992 QB1, the prototype 'cubewano' and the first 'Kuiper Belt' object.
- 5. Pluto = minor planet (134340) now among several large trans-Neptunian objects (TNOs) classified as 'dwarf planets'; Pluto: the 'king' of the Kuiper belt.

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Persistent Puzzles of Comets

- 1. What are comets ... Are they all the same ... Or are some comets (e.g. long-period) different from others (e.g. short-period)?
- 2. How are comets formed, and where? For example, are comets formed in or beyond the protoplanetary region; or in the protostellar molecular cloud: or beyond, in interstellar space?
- 3. What is (or are) the proximate source(s) of observed comets?
- 4. What is the structure and evolution of the 'observed' Oort cloud; how was it formed: and does it contain a massive dense inner core?
- 5. What is the role of the newly discovered, large, outer solar system bodies: Centaurs, Edgeworth-Kuiper belt objects, trans-Neptunian objects etc?
- 6. What is the cometary mass function and average cometary mass? ... and how many comets are there, and what is their total mass?
- 7. Are comets fragile or strong; what are their end-states; and what is the impact of cometary debris on the planets, Earth and Sun? lorthumbria, NCL 1017 Sept 14 – #26

Evolution of Oort Cloud: Contrasting Views

1. 1950 Model: quasi-steady state; comets in long-term 'deep freeze' of Oort cloud for age of solar system; stars dominate the evolution; no dense inner core.

2 Modern view:

- On short timescales: $t \lesssim 10$ Myr: Changes in perihelion distance dominated by Galactic tide and passing stars; leads to a quasi-steady long-period comet flux; changes in orbital energy dominated by stellar perturbations.
- On medium timescales: $10 \lesssim t \lesssim 500$ Myr: periodic new-comet flux due to Sun's orbit about Galactic plan; rare, close stellar passages more important for randomizing orbits; changes in orbital energy still dominated by stars.
- On long timescales: $500 \lesssim t \lesssim 4000$ Myr: rare, close molecular cloud encounters disrupt outer cloud, dominating changes in orbital energy beyond c.10,000 AU; rare, close stellar encounters stir up inner core. Together, these major upheavals replenish the transition zone between inner and outer Oort cloud and stir up orbits in Dense Inner Core. Northumbria, NCL 2017 Sept 14 – #30

- 1. Two main types of external perturber: stars and molecular clouds. • Galactic tide also drives comets into inner solar system, but has little direct effect on Oort cloud's disruption.
- 2. Stars pass through and beyond the Oort cloud, causing gradual unbinding of cometary orbits; the 'stellar' half-life is $t_{1/2,*} \simeq 2 \times \left(2 \times 10^4 \text{ AU}/a\right) \text{ Gyr.}$
- 3. Molecular clouds pass beyond the Oort cloud, but are much more massive than stars; the 'molecular cloud' half-life is $t_{1/2,c}\simeq 2 imes \left(2 imes 10^4~{
 m AU}/a
 ight)^3~{
 m Gyr}$

 \implies 'standard Oort cloud dynamically unstable beyond $a\simeq 2 imes 10^4$ AU, over the age of the solar system $(4.5 \, \text{Gyr})$

The Oort cloud is a leaky reservoir which must be replenished from within, possibly the trans-Neptunian region or a Dense Inner Core.

- (Duncan, Quinn, & Tremaine, 1988): the 'classical' Kuiper belt.
 - Comets must have perihelia near Neptune, i.e. q ≈ 30 AU, in order to be efficiently captured and 'handed down' to the Jupiter family.
 Simulations require at least 4 × 10⁹ such comets in the comet belt, if
 - Simulations require at least 4 × 10° such comets in the comet belt, if this is the dominant source of JFCs.
 The <u>dynamical</u> lifetime of JFCs is ≈ 3 × 10⁵ yr; their <u>active</u> lifetime is
 - much shorter, i.e. $\approx 1.2 \times 10^4$ yr (otherwise inclinations increase).
- 3. Two main problems: (1) the required source orbits are not observed; and (2) evolution of an initial distribution of low-inclination Neptune-crossing orbits inevitably produces a 'Scattered Disc' containing a similar number of comets in much more eccentric low-inclination orbits. These are much more readily captured into JFC orbits.

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\implies JFCs primarily not from Kuiper belt, but from <u>Scattered Disc</u>.
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New Number Problems: Scattered Disc and Oort Cloud 1. Simulations require number of comets in Scattered Disc to be ≤10⁹. But best observational estimates of number in Scattered Disc are ≈ 1-2×10⁸, albeit with large uncertainty. 2. Simulations require number of comets in Oort Cloud to be approximately ten times the number in Scattered Disc, i.e. ≤10¹⁰. But best observational estimates of number in Oort Cloud ≥2×10¹¹. 3. Two recent 'solutions' (NB: ideas go back many years): > Observed JFCs not in steady state; or large Scattered Disc Objects tidally break up into many fragments during dynamical evolution towards JFCs (Volk & Malhotra 2008). > Observed Oort cloud not primordial to solar system, but instead comprises largely captured comets, e.g. ejected from the

comprises largely captured comets, e.g. ejected from the Scattered Discs of other stars making up our Sun's parent star cluster (Levison, Duncan, Brasser & Kaufmann 2010).

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New Discoveries: Complex Dynamical Evolution

- science; they have had a significant impact on the Earth and on the development of scientific ideas.
- 3. Earth is now viewed as an 'open' system in touch with its near-space environment: a paradigm shift as significant as Copernicanism.
- 4. Solar system 'very leaky' with important implications for the amount of dust, small bodies and planets within molecular clouds and the interstellar medium. For example, what about comet clouds around other stars?
- 5. Emerging Modern Picture of Comets: a balance between the historic catastrophist and subsequent uniformitarian views; i.e. comets as destroyers of life <u>AND</u> as bodies that bring the necessities of life (e.g. water, organics, perhaps seeds of life itself) to Earth.

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Cometary Impacts Through Time?

- Ancient history suggests 'the sky' may have been significantly different in proto-historic times (e.g. more 'active', more interplanetary debris, brighter zodiacal light etc.). How can that be?
- Cometary masses range up to the size of dwarf planets. what are the effects of occasional 'giants' on Earth (and Sun)? What is the average mass of a comet?
- 3. Are all comets essentially the same; or are there two or more different classes, e.g. depending on origin and/or dynamical characteristics?
- 4. Total mass of Oort cloud may be very large ($\approx 10^2 M_{\oplus} \text{ pc}^{-3}$). Does this lead to serious difficulties for the 'standard' primordial solar system picture?
- 5. 'Fading problem' still not understood, but effectively determines the predicted 1/a-distribution. What happens to the cometary debris?

6. Meteoroid streams initially very fine-grained. This implies strong time-dependence in accretion of dust and small bodies on Earth.

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Later Developments: Horoscopic Astrology to Science

- 3. Horoscopic Astrology (pprox400 BC to pprox1600 AD)
 - Based on the entirely false premise that wandering stars ('planets') exert a distant controlling influence on human affairs.
 - Provides an early example of a powerful, but 'magical' scientific concept, i.e. 'action at a distance'.
 - Motivates careful <u>observations</u> of the planets; their paths against the fixed stars; their periods of revolution etc; all linked to <u>predictions</u>.
 - Demonstrates growing understanding and an increasingly 'scientific' approach to observatons of the natural world;
 - Nevertheless, the focus on unimportant chance alignments of planets and stars, planetary conjunctions etc. (e.g. 'Star of Bethlehem'), and on the 'random' appearance of an occasional bright comet etc. ultimately proves to be a cul-de-sac for science.
- Despite this, the idea of horoscopic astrology has proved remarkably hard to shift: it's still believed by upwards of 25% of the population!
 Scientific Astronomy (≈1600 AD to present)
- \approx 5 clenting Astronomy (\approx 1000 AD to present)

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Comets in Astronomy and History

Competition between two main factors:

- 1. General advances in science and understanding that began in the Renaissance, i.e. the few centuries up to the Industrial Revolution;
 - Provide a backdrop against with to 'read' the literature on comets in the 17th–19th century and earlier;
 - End of the 18th century: a kind of 'watershed' between an older pre-scientific view of the natural world, and the modern 'scientific' view'.
- 2. A more or less continuous strand of interest in comets and cometary debris, from the earliest times right up to the present day, viz:
 - The physical and societal impact of comets;
 - Comets as agents of destruction (catastrophism) versus celestial bodies that convey(ed) ingredients necessary to sustain 'Life' on Earth;
 - The rejection and rediscovery of cometary catastrophism.

 \implies New paradigm: Earth in touch with its <u>near-space environment</u>.

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Foundations of Astrology

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- Four broad phases can be identified:
- 1. Judicial Astrology (\approx 3000–1000 BC)
 - Events in sky self-evidently influence events on Earth.
 - Celestial 'order' transmitted to Earth by sky-gods or deities.
 - $\blacktriangleright \implies$ a powerful 'motive' to observe the sky and interpret the celestial 'omens'.
 - The sky gods are 'announcing' events on Earth, for example through the appearance of a bright comet or meteor, or by the fall of a meteorite or thunderbolt hurled by the sky-god Jupiter etc.
- 2. Zodiacal Astrology (\approx 1000–400 BC)
 - A slow transformation from Judicial Astrology to an increasing focus on the important part of the sky associated with the principal sky-gods, i.e. the Zodiac.
 - The sky divided into sections, each with a different perceived 'influence' on people or events on Earth.

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Early Greek Ideas: Anaximander's Jets of Fire

- 1. Earth seen as a short, squat cylinder three times as wide as long, surrounded by air and floating freely at the centre of the observable Universe in an infinite space.
- Sun, planets, stars are enclosed circular hoops of fire <u>below</u> the Sun and Moon. They only become visible due to holes in their enclosing hoops that allow the fiery substance to leak out and become visible. There seems to be no rational explanation for this <u>surreal</u> view about the sky.

Romans and Etruscans: Seeing Comets/Meteors as Omens

- 1. Accurate astronomical observations are the key to predictions, and early Babylonian astronomers expanded their knowledge of planetary recurrence cycles to include meteors leading to the omen literature.
- Resulting prophecies always took the form "If [astronomical observation] then [terrestrial effect]", e.g. Bjorkman (*Meteoritics*, 8, 91, 1973): "<u>If</u> a shooting star flashes as bright as a light or as a torch from east to west and disappears on the horizon, <u>then</u> the army of the enemy will be slain in its onslaught"

What could have motivated these ideas? Seneca (c.4 BC – 65 AD) gives some insight. Referring to the difference between 'us' Romans and the former Etruscans, he remarks, "... Whereas we believe that lightning is caused by clouds colliding, they believe that clouds collide in order to create lightning. Since they attribute everything to the gods, they are led to believe not that events have a meaning because they have happened, but that they happen in order to express a meaning."

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Problems with Lyttleton's Theory

- 1. Dust clouds do not exist on their own. The interstellar dust is dominated (by a mass fraction of at least a factor of 50) by hydrogen gas. Effects of gas must be included; this was never done.
- 2. The supposed proto-comets are far too small. Even if an accretion stream could be set up, only very short segments of length $d(r) \lesssim 2\sqrt{\mu r^3/M_{\odot}}$ at heliocentric distance r could successfully contract against the tidal field of the Sun. This leads to $m_c \lesssim 10^8 (10 \, {\rm km \ s^{-1}}/V)^9 (
 ho_{\rm dust}/10^{-22} \, {\rm kg \ m^{-3}})^{3/2} \, {\rm kg}.$
- 3. Inital orbits too short period and too anisotropic. Lyttleton argues for a long period of randomisation of orbits following the last accretion episode, but then the predicted 1/a-distribution quite wrong (diffusion theory).
- 4. The supposed proto-comets are on initial orbits directed towards Sun (or solar-system barycentre). All the initial comets will fall onto the Sun, unless inhomogeneities or planetary perturbations are invoked to deflect the stream.

In summary, despite strong advocacy of theory by Lyttleton for next $30\,$ years: "The theory is disproved: an honourable fate for a good theory"!

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Heuristic Results

1. Mean relative velocity change in a single encounter is approximately:

$$\Delta v = \frac{2GM}{bV} \begin{cases} \sqrt{2} & b < \sqrt{7/12} a \\ \sqrt{7/6} a/b & b > \sqrt{7/12} a \end{cases}$$

2. On short timescales (e.g. $t \lesssim 30$ Myr), the closest stellar encounter expected during a given time interval t has impact parameter $b_{\min} \simeq (2\pi nVt)^{-1/2}$, where n is the number density of perturbers. For stars this usually implies $b \gtrsim a$, which leads to

 $\Delta v_{max} \simeq 4\pi (7/6)^{1/2} G
ho at$

where $\rho = nM$ ($\approx 0.05 M_{\odot} \text{ pc}^{-3}$ for stars) is the mass density of perturbers.

- 3. This leads to $\Delta \nu_{\rm max} \simeq 4.3\,(a/3\times 10^4\,{\rm AU})(t/10\,{\rm Myr})$ m s $^{-1}.$
- 4. Finally, setting $t = P(a) \simeq 5.2 (a/3 \times 10^4 \text{ AU})^{3/2}$ Myr, the maximum change in perihelion distance during a single revolution can be shown to be of the order of $\Delta q \approx 5 (a/3 \times 10^4 \text{ AU})^{7/2} (q/1 \text{ AU})^{1/2}$ AU

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and

Time-Scales For Survival

1. For stars and $t \simeq 4.5$ Gyr, we have $a \gg a_c$. This implies $\dot{\epsilon}_* \approx \text{const.}$.

- 2. For molecular clouds and $t \simeq 4.5$ Gyr, we have $a \ll a_c$, i.e. $\dot{\varepsilon}_c \propto a^2$.
- 3. The net result is:

 $\dot{\varepsilon} = \dot{\varepsilon}_* + \dot{\varepsilon}_c \simeq A_* + A_c a^2$

where for typical parameters $A_* \simeq 10^{-13} \mbox{ m}^2 \mbox{s}^{-3}$ and $A_c \approx 10^{-44} \mbox{ s}^{-3}.$

4. Solving the energy evolution equation for each type of perturber leads to the half-life due to stellar and molecular cloud perturbations, i.e.

$$t_{1/2,*} = rac{1}{4.732} rac{GM_{\odot}}{A_* a} \simeq 2 imes 10^9 \left(rac{2 imes 10^4 \, {
m AU}}{a}
ight) \, {
m yr}$$

$$t_{1/2,c} = \frac{1}{8.190} \frac{GM_{\odot}}{A_c a^3} \simeq 2 \times 10^9 \left(\frac{2 \times 10^4 \text{ AU}}{a}\right)^3 \text{ yr}$$

5. Thus, due to both clouds and stars, the majority of comets with initial $a \gtrsim 2 \times 10^4$ AU will be lost. This is the Oort cloud survival problem. Northumbria, NCL 2017 Sept 14 – #79

Survival Problem: Physics of External Perturbations

1. Consider a perturber of mass M passing Sun with velocity \mathbf{V} and impact parameter **b** with respect to Sun and **d** with respect to a comet at heliocentric distance r.

Mean Energy Transfer Rate

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1. Change in orbital energy in a single encounter: let Δv be the relative velocity change of the comet with respect to the Sun, and let $\boldsymbol{v_0}$ be its orbital velocity, then

$$\Delta E = \mathbf{v}_{\mathbf{0}} \cdot \mathbf{\Delta} \mathbf{v} + \frac{1}{2} \, (\mathbf{\Delta} \mathbf{v})^2$$

Cometary orbital energies thus diffuse and systematically increase (i.e. become less tightly bound) owing to external perturbations.

2. Approximate result for point-mass perturbers: define $a_c = \sqrt{12/7} b_{
m min}$, where $b_{
m min} \simeq (2\pi nVt)^{-1/2}$ is the most probable minimum impact parameter for the perturbers of number density n, then the mean energy transfer rate can be shown to be approximately

$$\dot{\varepsilon}(t) = \frac{4\pi G^2 M^2 n}{V} \begin{cases} (a/a_c)^2 & a < a_c \\ 2\ln(a/a_c) + 1 & a > a_c \\ 2017 \text{ Sept } 14 - \#78 \end{cases}$$

Summary of Survival Problem: Oort Cloud Evolution 1. Two main types of external perturber: stars and molecular clouds. • Galactic tide also drives comets into inner solar system, but has little direct effect on Oort cloud's disruption. 2. Stars pass through and beyond the Oort cloud, causing gradual

- unbinding of cometary orbits; the 'stellar' half-life is $t_{1/2,*} \simeq 2 \times \left(2 \times 10^4 \,\text{AU}/a\right) \,\text{Gyr}.$
- 3. Molecular clouds pass beyond the Oort cloud, but are much more massive than stars; the 'molecular cloud' half-life is $t_{1/2,c}\simeq 2\times \left(2\times 10^4\,{\rm AU}/a\right)^3\,{\rm Gyr}$

 \implies 'standard Oort cloud dynamically unstable beyond $a \simeq 2 \times 10^4 \text{ AU}$, over the age of the solar system (4.5 Gyr)

The Oort cloud is a leaky reservoir which must be replenished from within, possibly the trans-Neptunian region or a Dense Inner Core.

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